A fuzzy approach for segmentation of touching characters

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Abstract

The problem of correctly segmenting touching characters is an hard task to solve. In the recent years, many methods and algorithms have been proposed without achieving a comprehensive solution. In this paper, a novel method based on fuzzy logic is studied. The proposed method combines three features of touching characters that in other studies have been exploited one at a time. The strategy is based on a 3–input/1–output fuzzy inference system with fuzzy rules specifically optimized for segmenting touching characters in the case of latin printed and handwritten characters. The system performances are illustrated and supported by numerical examples that show an optimal capability of segmenting touching characters. Moreover, numerical results suggest that the method can be applied to many different datasets of characters by means of a convenient tuning of the fuzzy sets and rules.

1   Introduction

Many studies deal with Optical Character Recognition systems (OCR) for the automatic recognition of both printed and handwritten characters. An OCR is composed by two main components: a pattern recognition algorithm and an image segmentation algorithm. The pattern recognition is the crucial step to allow a proper character recognition and leads the segmentation of an image to discover each single characters. In facts, errors in characters segmentation affect performance of the pattern recognition algorithm more than the degradation of the starting image [8].

One of the most difficult problem an image segmentation algorithm has to address is the segmentation of touching characters [26], [27]. Common techniques exploit different characterizing aspects of an image or the shape of the letters, such as vertical projection, pitch estimation or character size, contour analysis, or segmentation–recognition coupled techniques [13], [16]. Starting from these approaches, several methods have been developed for performing optimal segmentation of touching characters. Kurniawan et al. [11] identify touching positions in latin handwritten characters by means of self organizing feature maps and a region–based approach. Different approaches involving thinning algorithms can be found in [15] and [24]. In [30], Sharma et al. study the problem to detect arbitrarily-oriented text from video frames. Cut positions in touching characters are evaluated using the top distance profile. In [33] and [28], authors developed approaches by using genetic algorithms. Rehman et al. [25] identify character boundaries in an image by using a set of heuristic rules. The water reservoir algorithm has been exploited in some works like [23]

and [12]. Further methods can be foud in [1], [3], [34]. It is worth mentioning that some authors in [21] and [4] also deal with segmenting mathematical expressions.

Generally, these strategies consider binarized images where the patterns are represented by a matrix whose entries are 0 (white pixels) and 1 (black pixels). Then, a function identifies the cutting position for each column of the matrix by evaluating some features that characterize typical character positions in the text. These cut positions are chosen depending on these values. Common functions implied are the ratio of the second difference of the vertical projection (e.g., [9]) and the peak–to–valley (e.g., [14]). Other functions are, e.g., based on number of black pixels, number of white pixels counted from the top of the column to the first black pixel, crossing count (i.e., number of black to white transitions), number of identical black (white) pixels with left (right) column, width to height ratio for the remaining left (right) pattern after cutting (e.g., [2]). Another approach can be found in [5], where the authors used the inverse crossing count, measure of blob thickness and degree of middleness for defining a function that identifies when a column, a row, or a diagonal is a cutting position.

However, the methods and approaches above mentioned do not provide a comprehensive answer to the problem of segmenting touching characters. Indeed, their performances are not ever optimal and they are affected by the specific set of characters involved in the segmentation. Presently, there not exists a standard approach for the segmentaton of touching characters. Thus, this is currently an active research field.

In this paper, we aim at combining some of the previous features, usually exploited one at a time, by means of an original fuzzy logic approach in order to improve performances in separating touching characters. Indeed, the selection of the features that characterize touching positions is an art rather than a technique. In other words, the selection of the features mainly depends on the experience of the authors. Thus, in this context, fuzzy logic can be very useful, since it is congenial to capture and to code expert–based knowledge in view of performing targeted simulations.

Fuzzy logic has been already exploited to perform image segmentation. For instance, Garain and Chaudhuri [5] used fuzzy multifactorial analysis to combine some of the features previously described. In [20], a survey on image segmentation techniques using fuzzy clustering is presented. Fuzzy logic has been also exploited for developing segmentation–recognition coupled techniques [6]. A non–linear fuzzy approach can be found in [29]. In [19], authors used edge corners and fuzzy logic to develop segmentation techniques exploited to break down Captcha. Further approaches can be found in [7], [18], [31], [32].

In this paper, we propose a novel fuzzy approach that differs from the state of the art in several aspects. Firstly, we combine by means of a fuzzy strategy some features that are not ever exploited together in previous works. Secondly, we develop an original strategy based on an inference system composed by 3–input/1–output with fuzzy rules specifically optimized for the purpose of separating touching characters in the case of latin printed and handwritten characters. The strength of our fuzzy strategy relies on the possibility to adjust its parameters in such a way that they can fit the characteristics of the data set. In other words, the parameters of the method are extracted a priori based on the different characters in the data set.

The inference engine is based on the Mamdani model with if–then rules, minimax set–operations, sum for composition of activated rules and defuzzification based on the centroid method. We have chosen the Mamdani model since it is congenial to capture and to code expert–based knowledge [17].

The paper is organized as follows. In Section 2, we present the fuzzy strategy conveniently developed for performing segmentation of touching characters. In section 3, we present the numerical results that show the effectiveness of the proposed method. Specifically, in Section 3.1, we describe the datasets used for simulations. Sections 3.2 and 3.3 are devoted to test the method on datasets of latin printed and handwritten characters,

respectively. Finally, in Section 4 we present the conclusion.

2 Fuzzy strategy

In the following, we only focus on binarized images. Indeed, an image can be binarized resorting on an empirically determined threshold by, e.g., the Otsu method [22] that is one of the most used. In a binarized image, a pattern can be represented by a matrix whose entries are 0 (white pixels) and 1 (black pixels). Generally, methods for segmenting touching characters define a function based on some features that characterize cut positions. Then, such a function is evaluated for each column (row, or diagonal) of the matrix and the cut position is chosen depending on these values. Classical functions of this kind are the peak–to–valley function g and the function h defined as

$$g(i) = \frac{V(l_i) - 2V(i) + V(r_i)}{V(i) + 1}, \quad h(i) = \frac{V(i-1) - 2V(i) + V(i+1)}{V(i)},$$

where $V(i)$ denotes the vertical projection function for the i-th column (row or diagonal), l_i and r_i are the peak positions on the left side and right side of i, respectively. The column with the highest value of g (or h) is identified as the cutting column. A further feature, that can suggests if the i–th column (row, or diagonal) can be a cut position, is the distance $f(i)$ between i and the center of the pattern. Indeed, generally, cutting columns are located near to the center of the pattern. In this section, we combine functions f, g, and h by means of a fuzzy strategy that conveniently balances these functions. For the sake of simplicity, in the following we describe the fuzzy strategy focusing only on vertical cuts, i.e., we focus only on columns of the patterns.

To design a suitable fuzzy strategy, some steps are required, so to introduce the notion of a fuzzy degree qualifying a column i to be a cut position: for short $\rho = \rho(i) \in [0, 1]$. In our model, the low values of ρ locate good cut positions. The strategy can be detailed by means of the fuzzification of the functions f, g, h.

Given a pattern in a binarized image, let A, m, n, and c be the matrix of pixels of the binarized image, the number of row of A, the number of column of A, and the central column of A, respectively. In the following, when we refer to a column i of A, we refer to the i–th column of A, i.e., we are considering the vector of length m whose elements are the entries of the i–th column or we are only considering its position. This will be clear from the context.

The central column c is evaluated by means of $c = \frac{n+1}{2}$. When n is odd, c is clearly the central column of A; when n is even, we consider as the central column the mean between $\frac{n}{2}$–th column and $\frac{n}{2} + 1$, even if in this case c is not an integer number. In this way, for each column i of A, we define its distance from the center of the pattern as $f(i) = |c - i|$. In our fuzzy strategy, we take into account the normalized distance between each column i and the central column c, i.e., we consider $\bar{f}(i) = \frac{f(i)}{c}$.

Similarly, for each column i of A, instead of the functions g and h, we consider the normalized functions

$$\tilde{g}(i) = \frac{g(i) - \min_{j \in \mathcal{C}} g(j)}{\max_{j \in \mathcal{C}} g(j) - \min_{j \in \mathcal{C}} g(j)}, \quad \tilde{h}(i) = \frac{h(i) - \min_{j \in \mathcal{C}} h(j)}{\max_{j \in \mathcal{C}} h(j) - \min_{j \in \mathcal{C}} h(j)},$$

where $\mathcal{C} = \{1, 2, ..., n\}$ is the set of the columns of A. Note that functions $\tilde{g}$ and $\tilde{h}$ are well–defined since we consider matrices A where at least two columns are different. Finally, in the following we will use the functions

$$\bar{g} = 1 - \tilde{g}, \quad \bar{h} = 1 - \tilde{h}$$

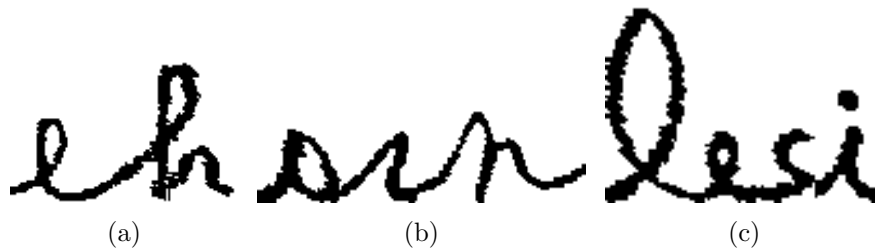so that low values of $\bar{g}$ and $\bar{h}$ identify cutting columns.

Figure 1: Samples of, respectively, two (a), three (b), and four (c) handwritten cursive touching character patterns.

Functions $\bar{f}$, $\bar{g}$, $\bar{h}$ are fuzzified by defining convenient fuzzy sets and related membership functions. The fuzzy degree ρ will be evaluated combining these functions by means of some fuzzy rules. Fuzzy sets, membership functions, fuzzy rules will be specified in sections 3.2 and 3.3.

The inference engine will be the basic Mamdani model [17], with if–then rules, mini-max set–operations, sum for composition of activated rules, and defuzzification based on the centroid method. The Mamdani model is congenial to capture and to code expert–based knowledge in view of performing targeted simulations; accordingly the system's performance is tuned by means of expert–based choices, heuristic criteria and non–linear optimization methods.

3   Experimental tests

Although create a specific data set of touching character is not our main contribution, the lacking of good examples on which we can work, force us to build a collection of touching characters. In particular, we create two different data sets, one with handwritten cursive characters, the other contains sided machine printed characters. In this section we present the preprocessing for the setting of the experimental tests. In the first part, we show these two dataset and we discuss our choices and methodology.

Due to the different characteristics of the data sets, chosen on purpose, in the remain parts of the section we discuss the process to select the best parameters for running our method on the two datasets. Our fuzzy strategy has a specif parameter meant to capture the difference between one dataset to another. Such parameters are tailored on the specific dataset characteristic by using an heuristic way and non–linear optimization methods.

Moreover, we would like to point out that the three features combined in our fuzzy routine seem to be sufficient for obtaining optimal results in the segmentation. In facts, adding further features appear to be useless. For instance, we have verified that the use of the crossing count as a fourth fuzzy input did not lead to improvements.

3.1   Construction of the datasets

As stated in many state-of-the-art work, e.g. [11], unfortunately at the present a comprehensive dataset specific on touching characters is still missing. Given that, for researches it is difficult to conduct experiment and to analyze any proposed method; in addition, it is hard to fair compare performances and results obtained from different authors. We try to overtake such an obstacle by proposing two datasets.

<div align="center">
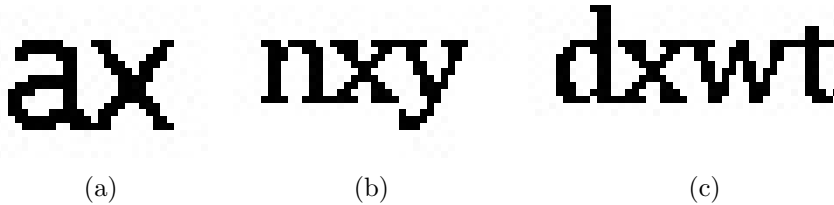
(a)   (b)   (c)

</div>

Figure 2: Samples of, respectively, two (a), three (b), and four (c) machine printed touching character patterns.

The first one is a dataset (dataset A) containing images of handwritten cursive characters we have built relying on samples from a standard dataset, in fashion of [11]. In particular we started from the CCC database [3]. The CCC database contains 57,293 samples of cursive characters that were manually extracted from images coming from different input sources, mainly related to American Post Services. They include both upper and lower case letters. Each sample is stored as a binary matrix within the database, and accompanied with information about the size of the matrix itself and the character that is represented. Starting from the whole database, we developed a MATLAB script to randomly extract 1'000 of its samples, taking care of maintaining a uniform distribution for all the characters chosen, both in their upper and lower version. These samples were later combined and merged together to form two, three, and four touching character patterns, each of whom is accompanied by a textual descriptor indicating the index of the proper cut column (or columns, in the case of three and four multiple touching character patterns). One sample of each category of patterns is shown in Figure 1. For instance, the descriptor of the sample represented in Figure 1a states that the proper column to cut to properly separate the "e" and the "h" characters is the 52th.

This merging is however unsupervised, and so improper combinations happen during the process. So, we had to filter out the most unrealistic ones. Firstly, we discarded all the samples with significant difference in their heights. Secondly, we manually removed combinations without touching patterns (i.e., the characters were well separated) or with touching patterns that seemed impossible to happen in real world. At the end, we kept 153 combinations, of which 139 represent two touching character patterns, and the other are equally divided into three and four touching character patterns. The disproportion because the common touching characters consist of two characters, while three or more touching characters are rare [33]. Moreover, note that the quantity of combinations of touching characters contained in our dataset is in compliance with other similar datasets constructed using the CCC database (e.g., in [11] a dataset of 123 touching characters is used).

The second one is instead a dataset (dataset B) containing images of sided machine printed characters we have built resorting on a second MATLAB script. We have identified a list of font types (namely Cambria, Candara, Georgia, Lucida Sans Regular, Times New Roman and Verdana Bold) and sizes (namely 10, 20 and 25); for each type and size the MATLAB script combines into images the lower characters from the alphabet to form two, three, and four touching character patterns. Each image is accompanied by a textual descriptor, which in this case indicates directly the characters represented. One sample of each category of patterns is shown in Figure 2. For instance, the descriptor of the sample represented in Figure 2a states that the images represent the string "ax". Also in this case, we preferred to revise manually the dataset to remove missing, or unrealistic, touching patterns. At the end, we kept the most promising 189 combinations (where 168 are composed by two touching characters), in order to define a challenging dataset to test our approach.

3.2   Tests on latin printed characters

In the following, we perform segmentation of touching characters from the dataset B of latin printed characters described in the previous section, accordingly to the fuzzy strategy described in section 2. Fuzzy sets and membership functions related to $\bar{f}$, $\bar{g}$ and $\bar{h}$ are defined accordingly to expert based choices. Moreover, their construction has been optimized by using the Particle Swarm Optimization (PSO) algorithm [10] in order to improve performances of our fuzzy strategy. Similarly the fuzzy rules (described in the following) are tuned using both heuristic criteria and the PSO algorithm.

Given a matrix A as defined in section 2, for each column i of A, $\bar{f}(i)$, $\bar{g}(i)$ and $\bar{h}(i)$ are evaluated and the degree $\rho(i)$ is provided by the following inference scheme that includes three inputs (fuzzification of $\bar{f}$, $\bar{g}$, $\bar{h}$) and one output (cutting degree ρ). The column i with the lowest value of ρ is considered as the cut column.

The function $\bar{f}$ is fuzzified by defining the following fuzzy sets:

- if $\bar{f}(i) \leq 0.35$, then distance from the center of the pattern is *Low*;

- if $\bar{0}.15 \leq f(i) \leq 0.75$, then distance from the center of the pattern is *Medium*;

- if $\bar{f}(i) \geq 0.5$, then distance from the center of the pattern is *High*.

For the function $\bar{g}$, we define the following fuzzy sets:

- if $\bar{g}(i) \leq 0.4$, then $\bar{g}(i)$ is *Low*;

- if $0.2 \leq \bar{g}(i) \leq 0.5$, then $\bar{g}(i)$ is *Medium*;

- if $\bar{g}(i) \geq 0.45$, then $\bar{g}(i)$ is *High*.

The function $\bar{h}$ is fuzzified by means of the following fuzzy sets:

- if $\bar{h}(i) \leq 0.4$, then $\bar{h}(i)$ is *Low*;

- if $\bar{0}.1 \leq h(i) \leq 0.75$, then $\bar{h}(i)$ is *Medium*;

- if $\bar{h}(i) \geq 0.5$, then $\bar{h}(i)$ is *High*;

Figures 3, 4, and 5 show the membership functions of the previous fuzzy sets.

Finally, for the fuzzy output ρ we define the following fuzzy sets, whose membership functions are depicted in Figure 6:

- if $\rho(i) \leq 0.5$, then $\rho(i)$ is *Low*;

- if $0.4 \leq \rho(i) \leq 0.6$, then $\rho(i)$ is *Medium*;

- if $\rho(i) \geq 0.5$, then $\rho(i)$ is *High*;

The inference system is based on the following rules, that combine the three inputs $\bar{f}(i), \bar{g}(i), \bar{h}(i)$ in order to produce the fuzzy output $\rho(i)$, for each column i of A:

1. if $\bar{f}(i)$ is Low and $\bar{h}(i)$ is Low, then $\rho(i)$ is Low;

2. if $\bar{f}(i)$ is Low and $\bar{g}(i)$ is not High and $\bar{h}(i)$ is not Low, then $\rho(i)$ is Low;

3. if $\bar{f}(i)$ is Low and $\bar{g}(i)$ is High and $\bar{h}(i)$ is Medium, then $\rho(i)$ is Medium;

4. if $\bar{f}(i)$ is Medium and $\bar{h}(i)$ is not High, then $\rho(i)$ is Medium;

5. if $\bar{f}(i)$ is Medium and $\bar{g}(i)$ is Low and $\bar{h}(i)$ is High, then $\rho(i)$ is Medium;

6. if $\bar{f}(i)$ is High and $\bar{g}(i)$ is not High and $\bar{h}(i)$ is Low, then $\rho(i)$ is Medium;

7. if $\bar{f}(i)$ is High and $\bar{g}(i)$ is Low and $\bar{h}(i)$ is Medium, then $\rho(i)$ is Medium;

8. if $\bar{f}(i)$ is Low and $\bar{g}(i)$ is High and $\bar{h}(i)$ is High, then $\rho(i)$ is High;

9. if $\bar{f}(i)$ and $\bar{g}(i)$ and $\bar{h}(i)$ are not Low, then $\rho(i)$ is High;

10. if $\bar{f}(i)$ and $\bar{g}(i)$ are High, then $\rho(i)$ is High.

The touching characters in dataset B are correctly segmented in the 96.1% of the cases. For evaluating the correctness of the segmentation, we used a pattern recognition algorithm constructed by a neural network trained on the characters that compose the dataset B. We consider that touching character are correctly segmented when the pattern recognition algorithm correctly recognizes the characters after the segmentation.

Simulations show that the fuzzy combination of the functions f, g, h improves the correct identification of the cutting column with respect to their separated use.

To assess the performances of the fuzzy strategy compared to the usage on only the functions g and h, a numerical example is reported below. Let us consider the touching characters "vu" (font Times New Roman) depicted in Figure 7. Our fuzzy routine correctly identifies the cutting column as the column 12 which is assigned the minimum value of ρ among all the columns of the pattern. Specifically, we obtain $\rho(12) = 0.1924$. The fuzzy procedure performance is shown in Figure 8, with application to the column 12. On the other hand, both g and h separately locate the column 16 as the cutting column. Indeed, we can observe that, e.g., $h(16) = 8$ that is greater than $h(i)$, for $i = 1, ..., 21$, $i \neq 16$, for example $h(12) = 0$. In Table 1, we report the values of $\bar{f}, \bar{g}, \bar{h}, \rho$ for each column of the previous pattern (except for the first and the last column that are not surely cutting columns).

Table 1: Values of $\bar{f}$, $\bar{g}$, $\bar{h}$, ρ for the columns of the touching characters "vu" (excluded first and last column)

Column	$\bar{f}$	$\bar{g}$	$\bar{h}$	ρ
2	0.8182	0.4545	0.7778	0.7849
3	0.7273	0.6818	0.8333	0.8123
4	0.6364	0.8409	0.9167	0.7908
5	0.5455	0.8523	0.9111	0.8073
6	0.4545	0.8333	0.9333	0.8102
7	0.3636	0.6818	0.8148	0.7949
8	0.2727	0.6818	0.8889	0.8047
9	0.1818	0.6818	0.9259	0.8169
10	0.0909	0.5303	0.8889	0.8169
11	0	0.2273	0.7778	0.1984
12	0.0909	0.2273	0.8889	0.1924
13	0.1818	0.2273	0.1111	0.2078
14	0.2727	0.9343	0.9722	0.8047
15	0.3636	0.9205	1	0.7949
16	0.4545	0	0	0.5000
17	0.5455	0	0.7778	0.6305
18	0.6364	0.3788	0.9556	0.7302
19	0.7273	0.9091	0.9753	0.8123
20	0.8182	1	0.9877	0.8169

3.3 Tests on latin handwritten characters

In the following, we perform segmentation of touching characters from the dataset A of latin handwritten characters. Similarly to the previous section, fuzzy sets, membership functions, and fuzzy rules are defined accordingly to expert based choices and further optimized by the PSO algorithm. Features of the dataset A are greatly different from dataset B. For instance, touching positions in dataset B are often near to the center of the pattern. In the case of dataset A, cutting columns may occur more frequently at high
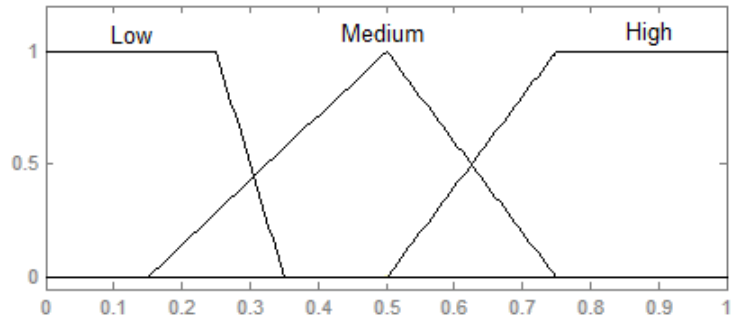
Figure 3: Membership functions of the fuzzy sets related to $\bar{f}$ (for dataset B)
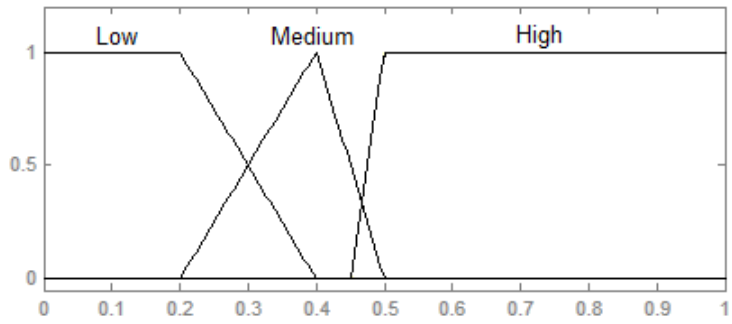

Figure 4: Membership functions of the fuzzy sets related to $\bar{g}$ (for dataset B)
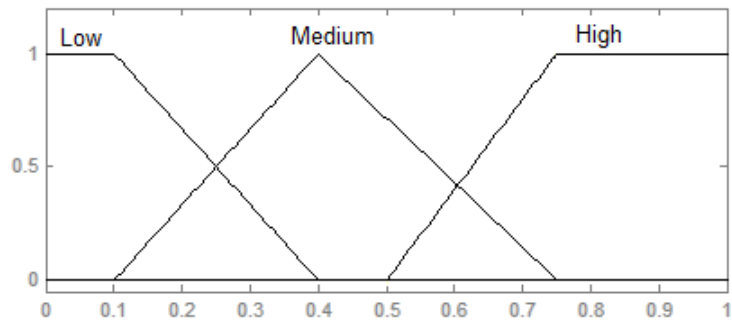

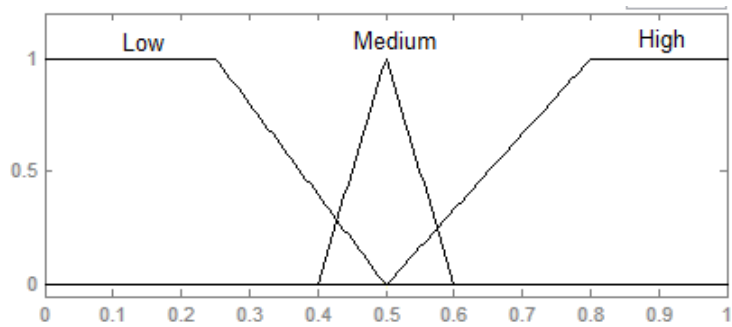Figure 5: Membership functions of the fuzzy sets related to $\bar{h}$ (for dataset B)

Figure 6: Membership functions of the fuzzy sets related to ρ (for dataset B)

distance from the center. On the other hand, the peak to valley function seems to have better performances in the case of the dataset A. Moreover, the optimization conducted by using the PSO algorithm allows to highlight properties and connections among functions f, g, h not noticeable at a glance. All these features are reflected in the following definition of fuzzy sets, membership functions, and fuzzy rules.

The fuzzy sets related to $\bar{f}$ are defined by

- if $\bar{f}(i) \leq 0.45$, then distance from the center of the pattern is *Low*;

- if $\bar{0}.25 \leq f(i) \leq 0.55$, then distance from the center of the pattern is *Medium*;

- if $\bar{f}(i) \geq 0.5$, then distance from the center of the pattern is *High*.

For the function $\bar{g}$, we define the following fuzzy sets:

- if $\bar{g}(i) \leq 0.2$, then $\bar{g}(i)$ is *Low*;

- if $0.15 \leq \bar{g}(i) \leq 0.55$, then $\bar{g}(i)$ is *Medium*;

- if $\bar{g}(i) \geq 0.25$, then $\bar{g}(i)$ is *High*.

The fuzzy sets related to $\bar{h}$ are defined by

- if $\bar{h}(i) \leq 0.3$, then $\bar{h}(i)$ is *Low*;

- if $\bar{0}.15 \leq h(i) \leq 0.65$, then $\bar{h}(i)$ is *Medium*;

- if $\bar{h}(i) \geq 0.5$, then $\bar{h}(i)$ is *High*;

Figures 9, 10, and 11 show the membership functions of the previous fuzzy sets.

Finally, for the fuzzy output ρ we define the following fuzzy sets, whose membership functions are depicted in Figure 12:

- if $\rho(i) \leq 0.4$, then $\rho(i)$ is *Low*;

- if $0.2 \leq \rho(i) \leq 0.65$, then $\rho(i)$ is *Medium*;

- if $\rho(i) \geq 0.4$, then $\rho(i)$ is *High*;

The inference system is based on the following rules, that combine the three inputs $\bar{f}(i), \bar{g}(i), \bar{h}(i)$ in order to produce the fuzzy output $\rho(i)$, for each column i of the matrix of pixels:

1. if $\bar{f}(i)$ is not High and $\bar{g}(i)$ is not High and $\bar{h}(i)$ is Low, then $\rho(i)$ is Low;

2. if $\bar{f}(i)$ is Low and $\bar{g}(i)$ is Low and $\bar{h}(i)$ is Medium, then $\rho(i)$ is Low;

3. if $\bar{f}(i)$ is Low and $\bar{g}(i)$ is High, then $\rho(i)$ is Medium;

4. if $\bar{g}(i)$ is Medium and $\bar{h}(i)$ is Medium, then $\rho(i)$ is Medium;

5. if $\bar{f}(i)$ is High and $\bar{g}(i)$ is Low, then $\rho(i)$ is Medium;

6. if $\bar{f}(i)$ is Medium and $\bar{g}(i)$ is Low and $\bar{h}(i)$ is Medium, then $\rho(i)$ is Medium;

7. if $\bar{f}(i)$ is High and $\bar{g}(i)$ is Medium and $\bar{h}(i)$ is Low, then $\rho(i)$ is Medium;

8. if $\bar{f}(i)$ is Medium and $\bar{g}(i)$ is High, then $\rho(i)$ is High;

9. if $\bar{f}(i)$ is High and $\bar{g}(i)$ is High, then $\rho(i)$ is High;

10. if $\bar{f}(i)$ is High and $\bar{g}(i)$ is Medium and $\bar{h}(i)$ is High, then $\rho(i)$ is High.
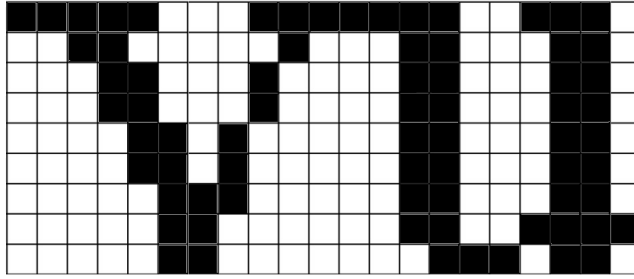
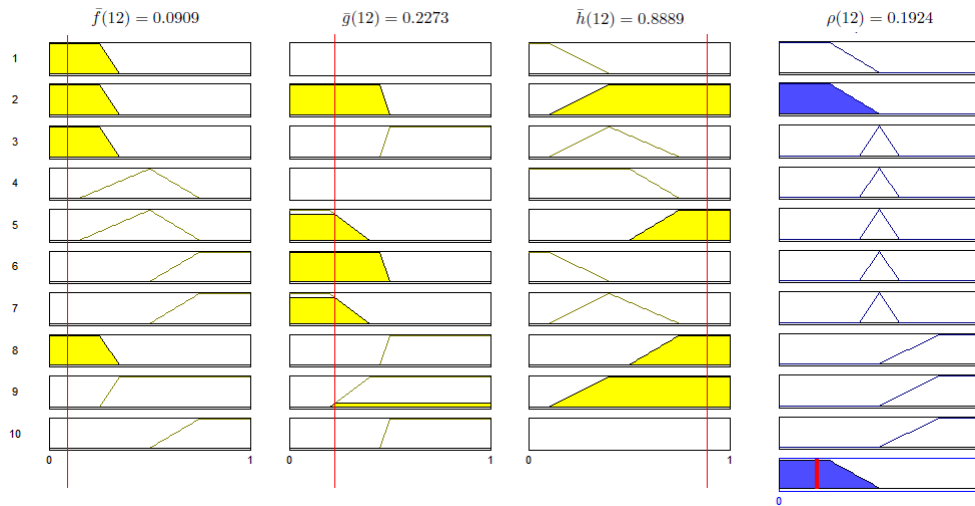Figure 7: Touching characters "vu" font Times New Roman

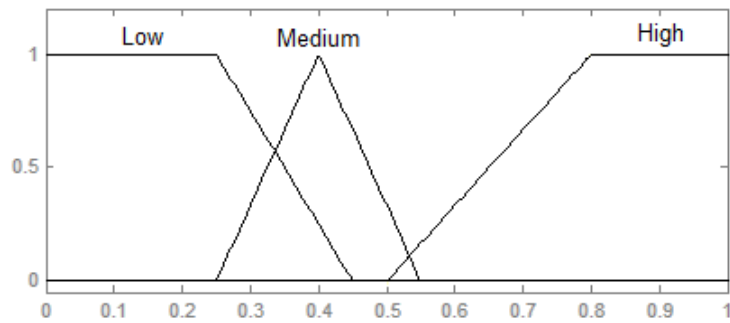Figure 8: Application of the fuzzy inference system to the column 12 of the pattern "vu"

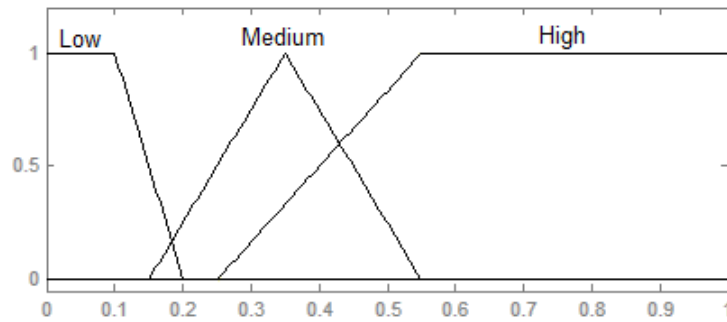Figure 9: Membership functions of the fuzzy sets related to $\bar{f}$ (for dataset A)

Figure 10: Membership functions of the fuzzy sets related to $\bar{g}$ (for dataset A)

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The touching characters in dataset A are correctly segmented in the 81.1% of the cases. Let us remember that in dataset A we have stored the textual descriptor indicating the index of the proper cut column. We consider a correct segmentation when the routine locates such a column. Let us note that CCC database provides a challenging set of characters for segmentation purposes. The only reference, where segmentation of touching characters obtained from CCC database is performed similarly to this section, is [11] whose authors obtained correct segmentation in the 76.2% of the cases. Moreover, authors considered percentage of inaccurate segmentation (i.e., when a cutting column is found around the correct position; specifically we consider inaccurate segmentation when the cut position is distant at most 5 columns from the exact position). In this case, percentage of segmentation increases to 91.9%, whereas we get 88.9%. Let us observe that these results are not well comparable, since our dataset A and dataset used in [11] are different, even if they are obtained starting from the same CCC database.

Some numerical results showing the behavior of our method are reported below, where segmentation is performed on touching characters "eh", "rt", "xm", and "ao" depicted in Figures 1a, 13a, 13b, and 13c, respectively.

For the touching characters "eh", our fuzzy routine identifies the correct cutting column as the column 52, whereas function $\bar{f}$ assumes the lowest value in correspondence of the column 56, function $\bar{g}$ in correspondence of columns 34,35,36,37, and function $\bar{h}$ in correspondence of the column 15.

For the touching characters "rt", our fuzzy routine identifies the correct cutting column as the column 61, whereas function $\bar{f}$, $\bar{g}$, and $\bar{h}$ identify the cutting position in correspondence of the columns 51, 61, and 70, respectively.

For the touching characters "xm", our fuzzy routine identifies the correct cutting column as the column 75, whereas function $\bar{f}$, $\bar{g}$, and $\bar{h}$ identify the cutting position in correspondence of the columns 79, 72, and 137, respectively.

Finally, for the touching characters "ao", our fuzzy routine identifies the correct cutting column as the column 43, whereas function $\bar{f}$ assumes the lowest value in correspondence of columns 48 and 49, function $\bar{g}$ in correspondence of the column 38, and function $\bar{h}$ in correspondence of the column 43.

In Figures 14 and 15, we show the cutting columns found by ρ, $\bar{g}$, and $\bar{h}$ related to touching characters "eh" and cutting columns found by ρ, $\bar{f}$, $\bar{h}$ related to touching characters "rt", respectively.

Note that we do not report values of ρ, $\bar{f}$, $\bar{g}$, $\bar{h}$ for each column since these patterns have usually more than 100 columns.

4   Conclusion

A fuzzy approach for segmentation of touching characters has been presented. The proposed method combines three classical features of touching characters usually exploited one at a time. Experiments have been conducted on two very different datasets composed by latin printed and handwritten characters, respectively. Fuzzy sets, membership functions, and fuzzy rules, which characterize the fuzzy inference scheme, have been properly constructed by means of expert–based choices, heuristic criteria, and the PSO algorithm for each dataset. Numerical results are encouraging and show that the proposed method has an optimal capability of correctly separating touching characters and may be adjusted for very different varieties of characters (not only for the types considered in simulations). Moreover, the present study shows that the simple functions f, g, h can be sufficient to manage the segmentation of touching characters. In fact, some experiments (not presented here) show that addition of other inputs in the fuzzy routine does not provide significant improvements. This is surely a perspective that should be further investigated and motivated. Indeed, looking at perspective advancements, the following issues could

be addressed in future works:

- study of characterization of performance improvements when adding further features as inputs in the fuzzy inference system;

- experiments on further datasets not involving latin characters;

- experiments on segmentation of formulae;

- use of fuzzy models different form the Mamdani one (as, e.g., the Sugeno model).

Acknowledgments

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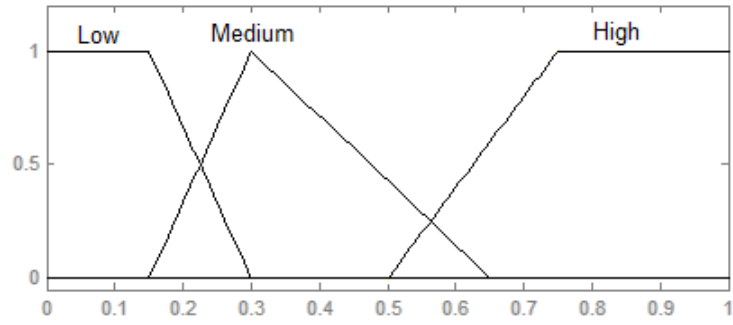
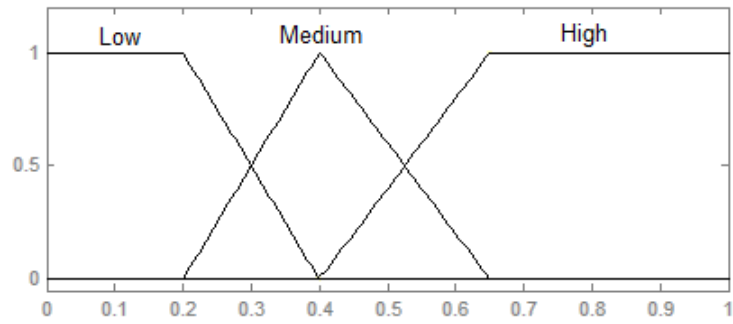Figure 11: Membership functions of the fuzzy sets related to $\bar{h}$ (for dataset A)

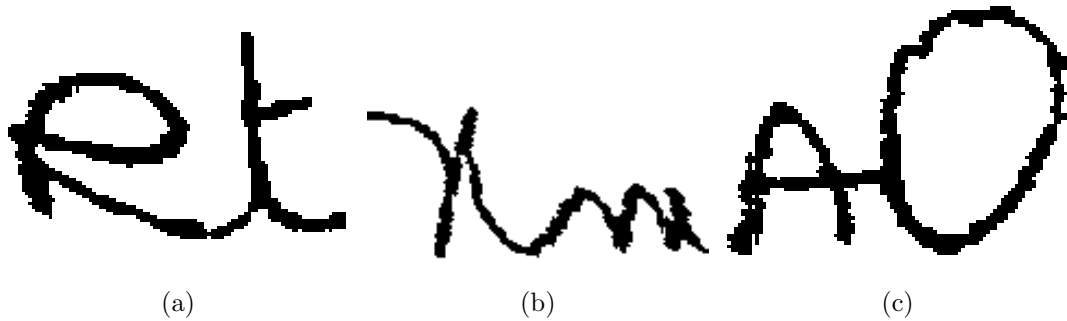Figure 12: Membership functions of the fuzzy sets related to ρ (for dataset A)

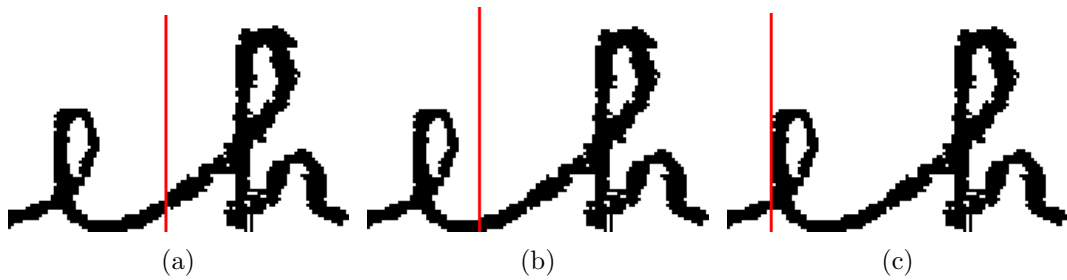Figure 13: Touching characters "rt", "xm", and "ao" extracted from the CCC database.

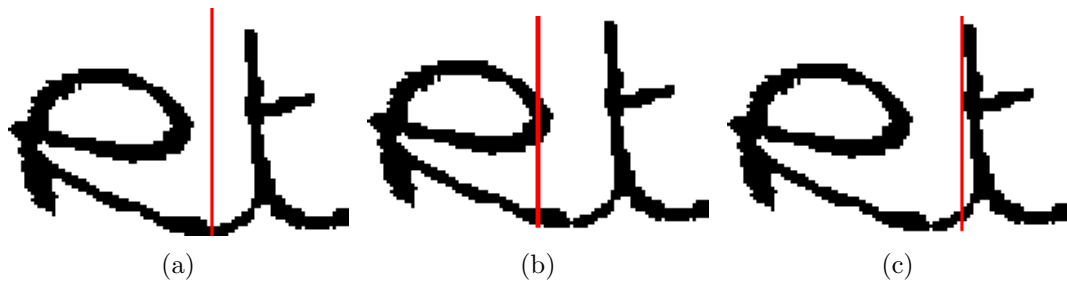Figure 14: Cutting postions located by ρ (a), $\bar{g}$ (b), and $\bar{h}$ (c).

Figure 15: Cutting postions located by ρ (a), $\bar{f}$ (b), and $\bar{h}$ (c).